

# Production of Membership functions for the high precision applications in fuzzy systems and neural networks

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**Abstract**— in this paper the circuit to produce the current mode membership function including OTA and MIN, MAX circuits has been presented. The ability to produce very linear triangular, trapezoidal, s-shape and z-shape functions for applications of neuron-fuzzy programming with controlling voltages is applied. The circuit is designed with simple structure, high dynamic range, low power consumption and area is the speed and accuracy is high. At the end the simulation results with the software HSPICE (49 levels) of 0.35 $\mu$ m CMOS standard processes is presented. Layout of circuits on the surface is about 5 $\mu$ m $\times$ 36  $\mu$ m.

**Keywords:** fuzzifier, Fuzzy controllers (FLC), Neuro-Fuzzy, OTA structure, membership function circuit

## I. INTRODUCTION

The design of fuzzy systems by Professor Lotfi Zadeh, that uncertainty of physical phenomena introduced, it was started. Fuzzy controllers (FLC) in a variety of control systems for easy and does not need accurate mathematical models are used. Fuzzy systems may be either a software or hardware used. The software can be effective when the speed and capacity is not needed, which is generally on the implementation of software systems of Neuro-Fuzzy has focused. The software is not suitable for high speed applications, so for solution of problem the hardware method (designed IC) for design is used. The analog circuits because used of parallel Structures are with high speed that the speed limit in this circuit is only due to the delay signal transmission system and also due to the low number of transistors and low-volume analog system to digital system used analog system. In the paper produced four types of membership functions using OTA structure has been studied.

CMOS circuitry for systems of FLC has been presented in recent papers; each has with advantages and disadvantages. fuzzifier circuits presented in reference [3] and [5] are unable to produce the sigmoid functions and their simultaneous production cause increase power consumption and increase

The area. In reference [3] as well as the increase current resources and number of transistors to increase the outputs, power consumption and Area is more. fuzzifier circuit presented, is an OTA-based circuits with MIN, MAX circuits that is flexible programming capability, high accuracy and dynamic range, low power consumption and simple structure

OTA structure is described in Section 2; in section 3, circuit to produce slope and How to change their slope; in Section 4; the MIN, MIN circuits, layout and circuit simulation in Section 5 and conclusions are presented in Section 6.

## II. THE OTA STRUCTURE

In general, fuzzy systems are composed of three main parts:

- A. *membership function circuit (Fuzzifier)*
- B. *apply the fuzzy rules, singleton and consequent circuits*
- C. *defuzzify*

Different functions in the fuzzy used that in this paper to produce four of them (triangle, trapezoid, s-shape, z-shape) is mentioned. To Production functions for the blocks listed in Figure 1, we perform:

And for the production of membership functions, s-shape and z-shape as the block (2) we pass the output of an OTA circuit of MAX and then MIN circuit.

## III. MEMBERSHIP FUNCTION CIRCUIT

- A. *slope circuit:*

Circuit (Fig. 3) to produce a linear slope function is designed:

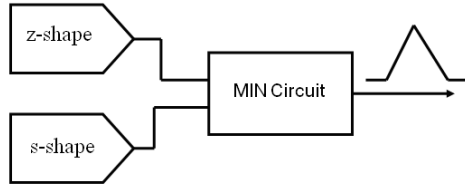


Figure 1. General block structure of the OTA

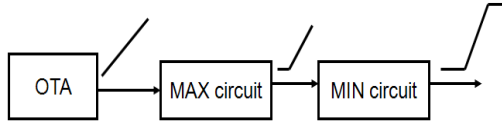


Figure 2. Block of s-shape and z-shape

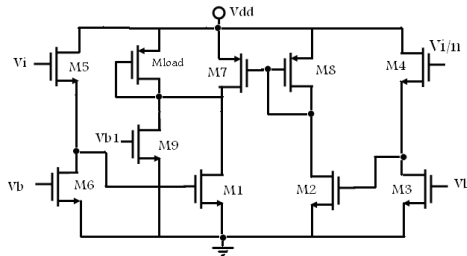


Figure 3. slope circuit

Transistors M3, M4, M5 and M6 as a buffer for Shift Register function on the horizontal axis to be used, so that the M3, M6, with gate-source voltage Vb, creating a current that must from the M4, M5 passes.

Thus the difference gate- source voltages of the M4, M5 are Vb and the gate voltages of the M4, M5 to Vb drops. If the process is only include Nwell for linearity more buffers (the body) can be used to Pwell.

$$V_i - V_x = V_b \Rightarrow V_x = V_i - V_b \quad (1)$$

At circuit in Figure 1 size of the transistor, M2 is equal  $n^2$  to the transistor M1 (n is ratio the input voltage) and the size of other transistors symmetrical by M1 transistor is placed. And The size of transistors Mload, M7, M8 also coincides. (Providing the bulk of the NMOS transistors are segregate, PMOS can be used)

In the circuit voltage applied to gate M1 creates a current that are the non-linear relationship (with a good approximation is a quadratic equation) with gate- source voltage and the generated Current by the M2 transistor is so designed that by the non-linear part of the transistor M1 is equal. Thus the current by mirror current M7 and M8 subtracted of the

current M1 and current linear part of transistor M1 is entered Mload.

In this case, the currents respect will be as follows:

$$I_1 = \frac{1}{2} \mu_n C_{ox} (w/l)_n (V_x - V_t)^2 \quad (2)$$

$$I_2 = \frac{1}{2} \mu_n C_{ox} (n^2 \times w/l)_n (V_x/n - V_t)^2 \quad (3)$$

$$I_2 = \frac{1}{2} \mu_n C_{ox} (w/l)_n \times (V_x^2 + n^2 \times V_t^2 - 2n \times V_x V_t) \quad (4)$$

That the current I2 drawn from M8 and is mirror the M7.

$$I_7 = I_2 \quad (5)$$

Id is current of M9 transistor.

$$I_{load} = I_1 - I_7 + I_d \quad (6)$$

$$I_{load} = \frac{1}{2} \mu_n C_{ox} (w/l)_n \times (2nV_x V_t - (n^2 + 1)V_t^2) + I_d$$

By situation  $V_x$  to  $V_i$  will be

$$I_{load} = \frac{1}{2} \mu_n C_{ox} (w/l)_n \times (2nV_i V_t - 2nV_b V_t - (n^2 + 1)V_t^2) + I_d \quad (7)$$

That in the relationship the current Iload varies linearly by Vi. By Vb for the shift on the horizontal axis and by id for the shift on the vertical axis is used.

Output OTA circuit is proposed as follows:

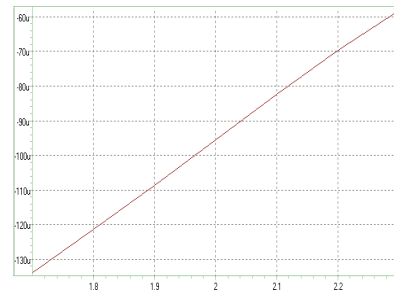


Figure 4. The sample of slope function produced by the OTA circuit

To determine the slope of membership function is made, two methods are provided:

1) When designing the slope of membership function can be determined by the size of transistors.

2) Changing the slope by control voltages that can be achieved by changing the threshold voltage by applying a voltage to the transistor bulk M1 and M2 is done.

As the simulation in Figure 5 shows the variation of current slope with increasing bulk's voltage, linearly decreased. But Since the high changes of bulk's voltage, current output be non-linear. Therefore amplitude of these changes should not be excessive. Relation of Bulk-source voltage and threshold voltage is as follows:

$$V_t = V_{t0} + \gamma(\sqrt{|2\phi_F| + V_{SB}} - \sqrt{|2\phi_F|}) \quad (8)$$

In relation (8)  $V_{t0}$  threshold voltage is the voltage per  $V_{SB} = 0$  is called zero threshold's voltage and Parameter gamma ( $\gamma$ ) is coefficient of the body (the body).

To obtain a negative slope, we decrease the output of circuit (3) from a constant dc current. In figure (5) Change the slope of the membership function per bulks voltage of zero and 0.4 is drawn:

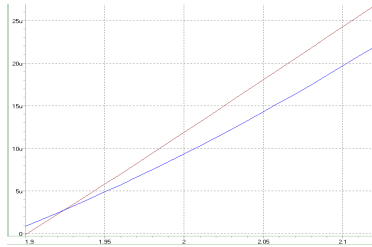


Figure 5. change of Slope of the production functions using the bulk voltage

For high linearity of circuit can the slope of the functions by the size of transistors in the design phase was determined.

#### IV. MAX AND MIN BLOCK

##### 1) MAX circuit

This circuit is to that it can be extended to more inputs. mechanism of the above circuit so that when the current  $I_{in1}$  is larger  $I_{in2}$  the voltage of node A and Consequently the node B and C will increase and because the current  $I_{in1}$  assumed is less than  $I_{in2}$  so Voltage nodes E and D, respectively, are lower than the voltage of node A and B. thus M3 due to less the voltage between drain and source of his enters into the linear region and M7 due to less the voltage between gate and source is cut off and maximum current through M5 to transmit output. (Of course providing the Differential input current is low; Transistor M3 can be at active area and the circuit works just as MAX circuit and the Differential current by reducing the voltage between the drain -source M3 is compensated)

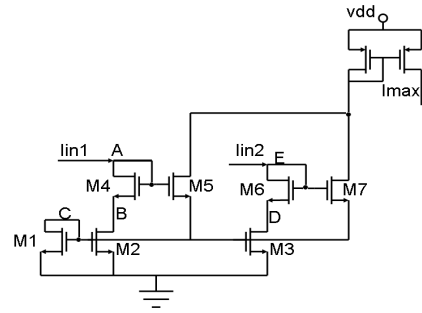


Figure 6. MAX circuit (All transistors have the same size)

##### 2) MIN circuit

MIN circuit presented providing in Figure (8). The mechanism of the above circuit so that first  $I_{in1}$  and  $I_{in2}$  currents through the  $I_d$  were complemented and their complement with MAX circuit is compared. That their maximum complementary of inputs will equal to the minimum input and Min current to transmit output.

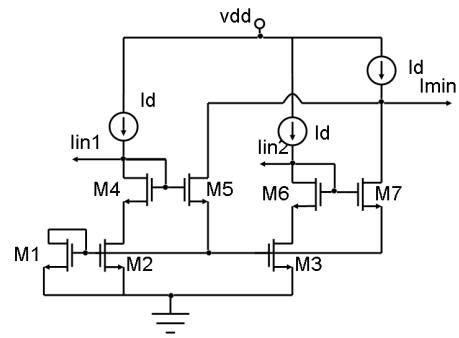


Figure 7. MIN circuit (inputs are Complemented and together compared )

#### V. SIMULATION RESULTS AND CIRCUIT LAYOUT

Simulation results using the Hspice software provided in the standard  $0.35\mu\text{m}$  CMOS. Total circuit power consumption is 200mw and dimensions of the layout are approximately  $15\mu\text{m} \times 36\mu\text{m}$ .

Membership functions are generated as follows:

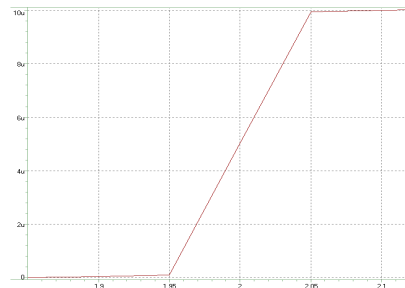


Figure 8. S-shape membership function

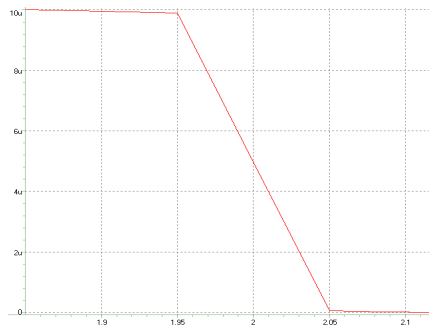


Figure 9. Z-shape membership function

In Figures 11 and 12 the ability to change the width and slope of membership function is shown:

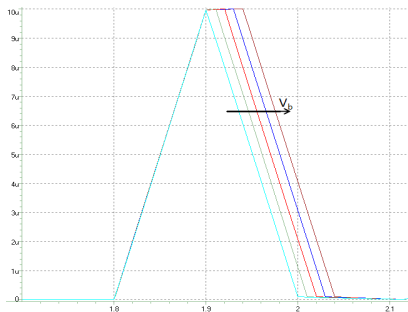


Figure 10. Change of width of the membership function

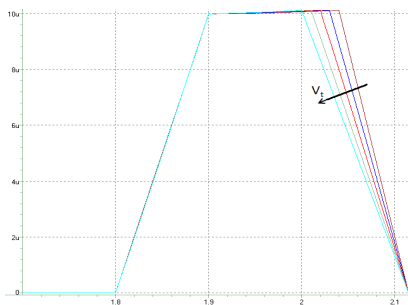


Figure 11. Change of Slope of the membership function

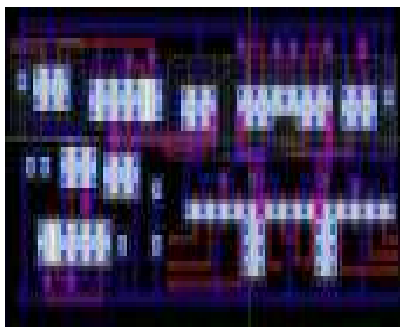


Figure 12. Circuit Layout

## VI. CONCLUSION

In the paper a circuit to produce a membership function programmable in CMOS technology is presented that can produce the four membership functions, triangular, trapezoid, z-shape, and s-shape. Linearity with very high accuracy is produced. The circuit designed moreover has the capability to increase the number of inputs and outputs with an increase in the small number of transistors. This reduces overall power consumption and chip area.

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